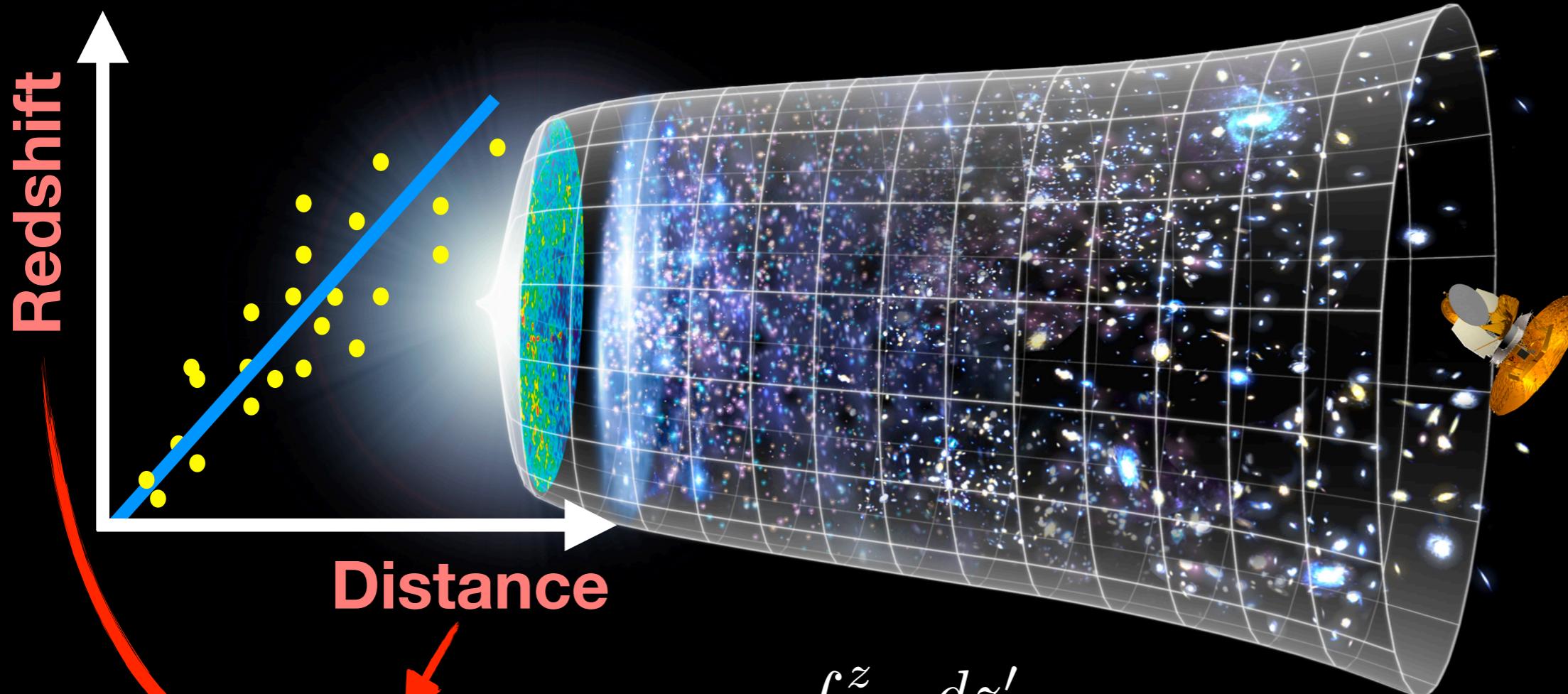


Tests of LCDM from WP perspective: methods and pipelines

Hsin-Yu Chen

The expansion history of the Universe

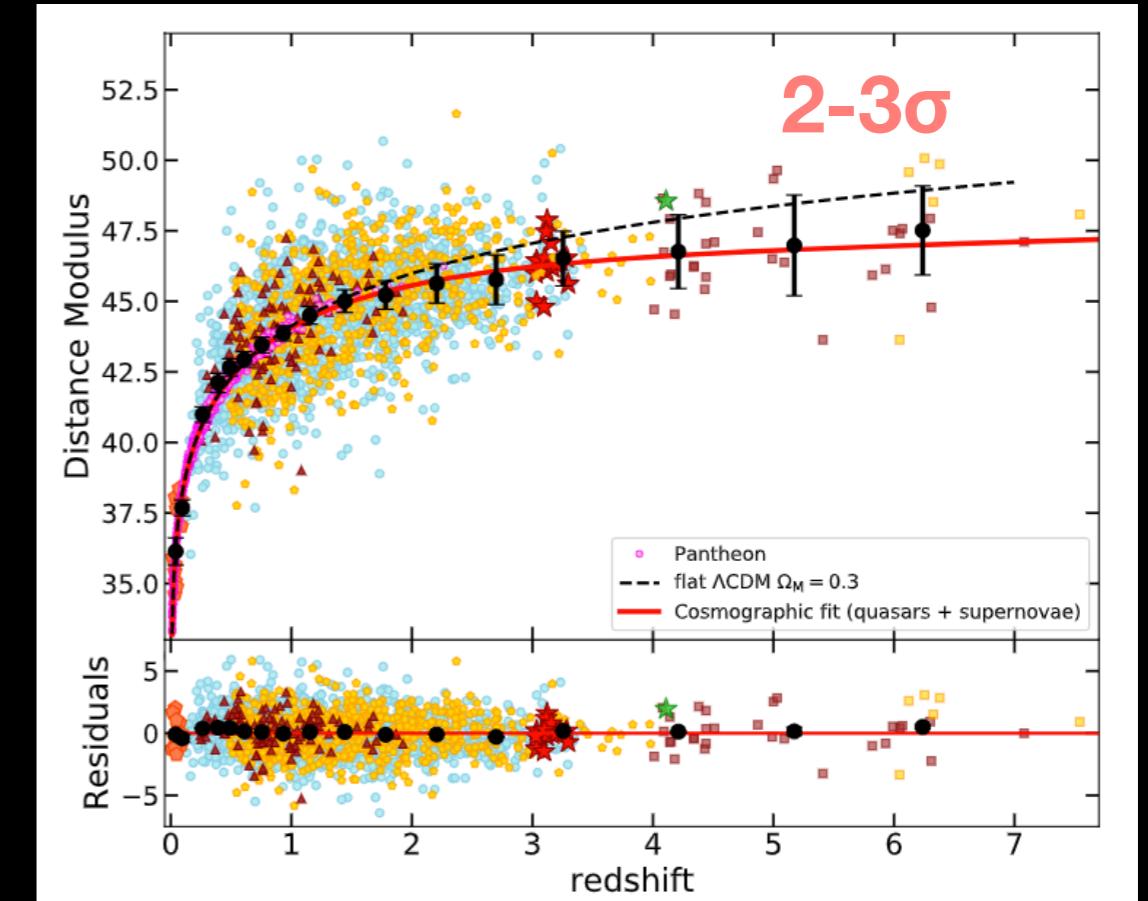
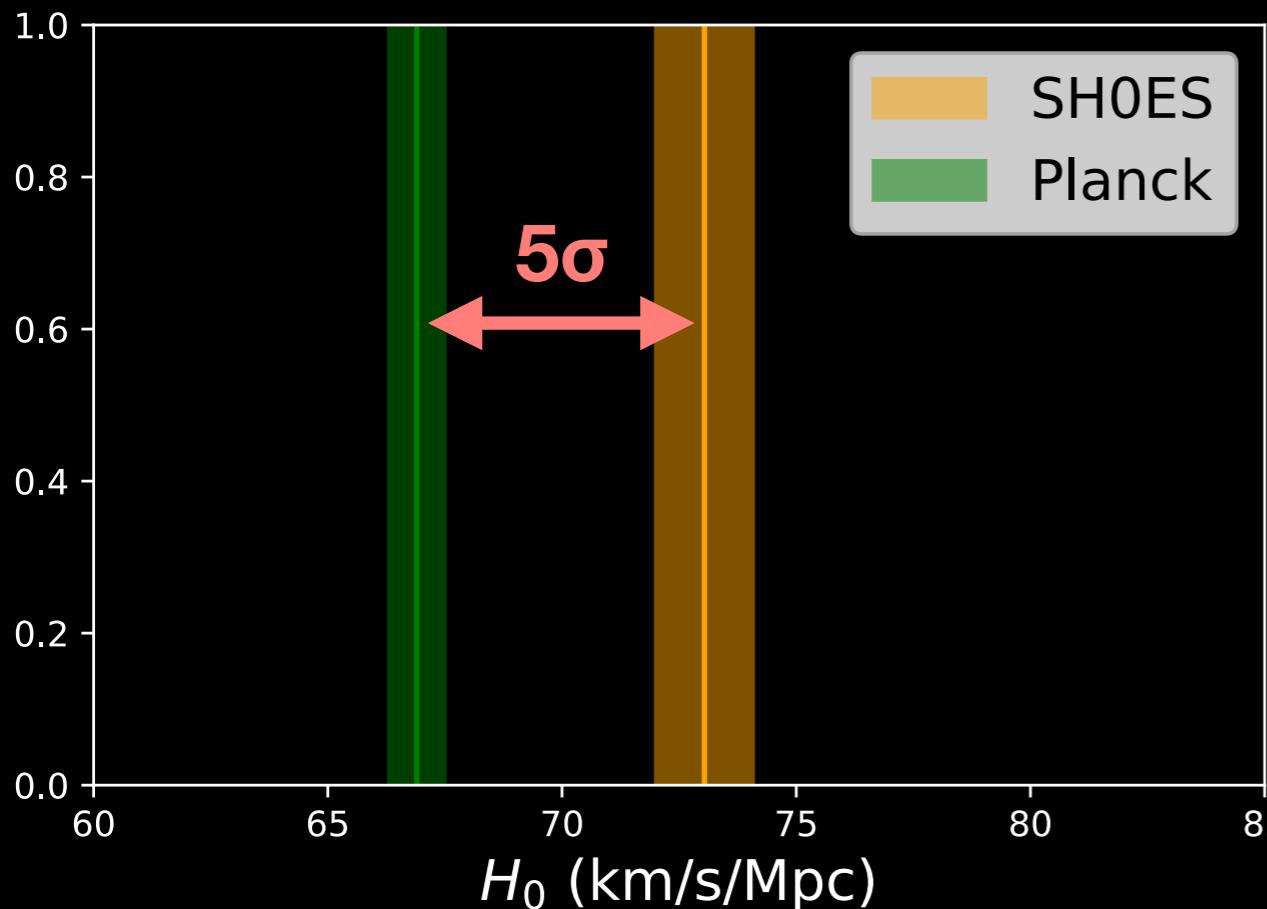


$$D_L = c(1+z) \int_0^z \frac{dz'}{H(z')}$$

$$H(z) = H_0 \sqrt{\Omega_M(1+z)^3 + \Omega_k(1+z)^2 + \Omega_\Lambda(1+z)^{3(1+w)}}$$

Astrophysical sources at different redshift range constrain different part of the expansion history.

Tensions in cosmological measurements

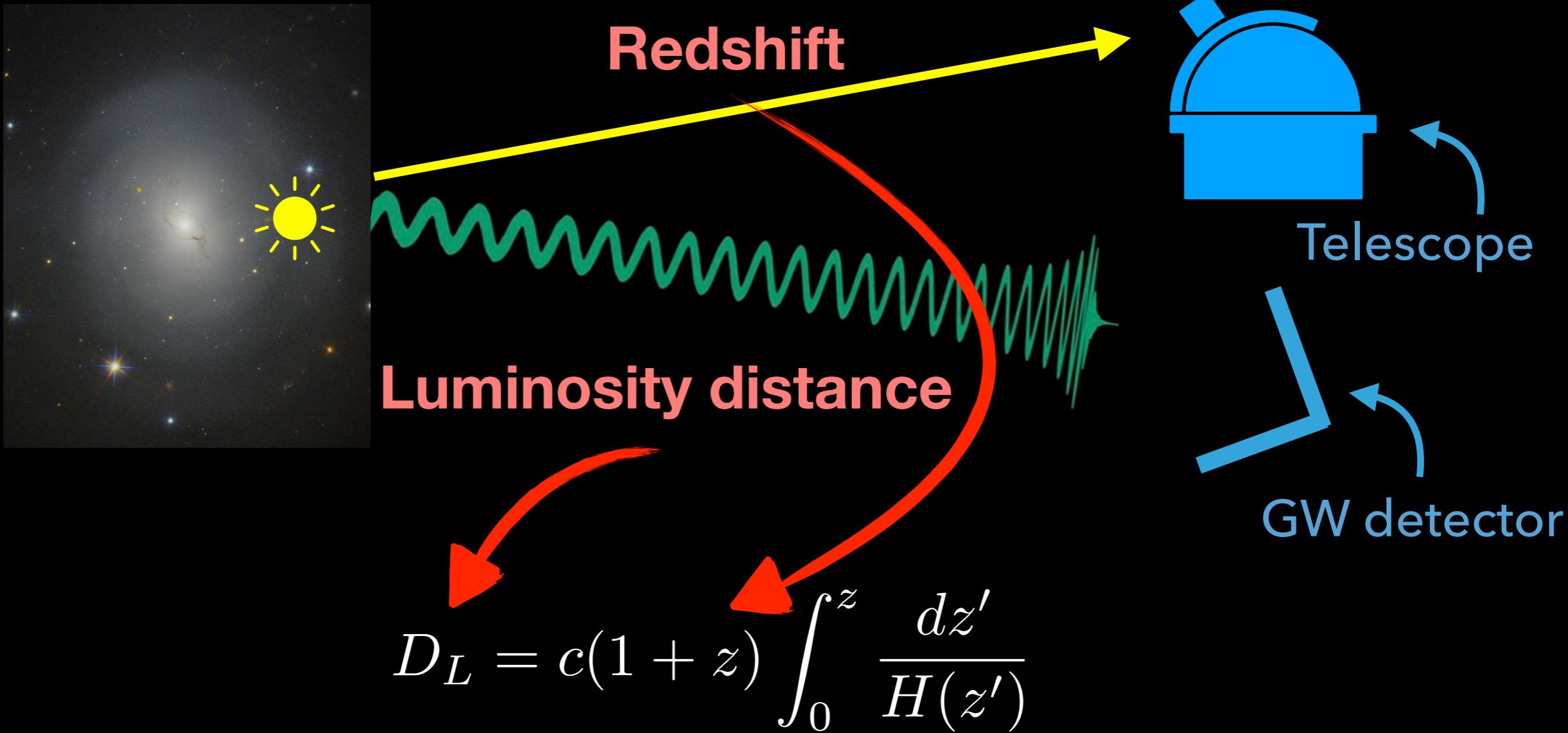


Lusso et al., A&A, 2020

Independent measurement of the cosmological parameters—
Standard siren method

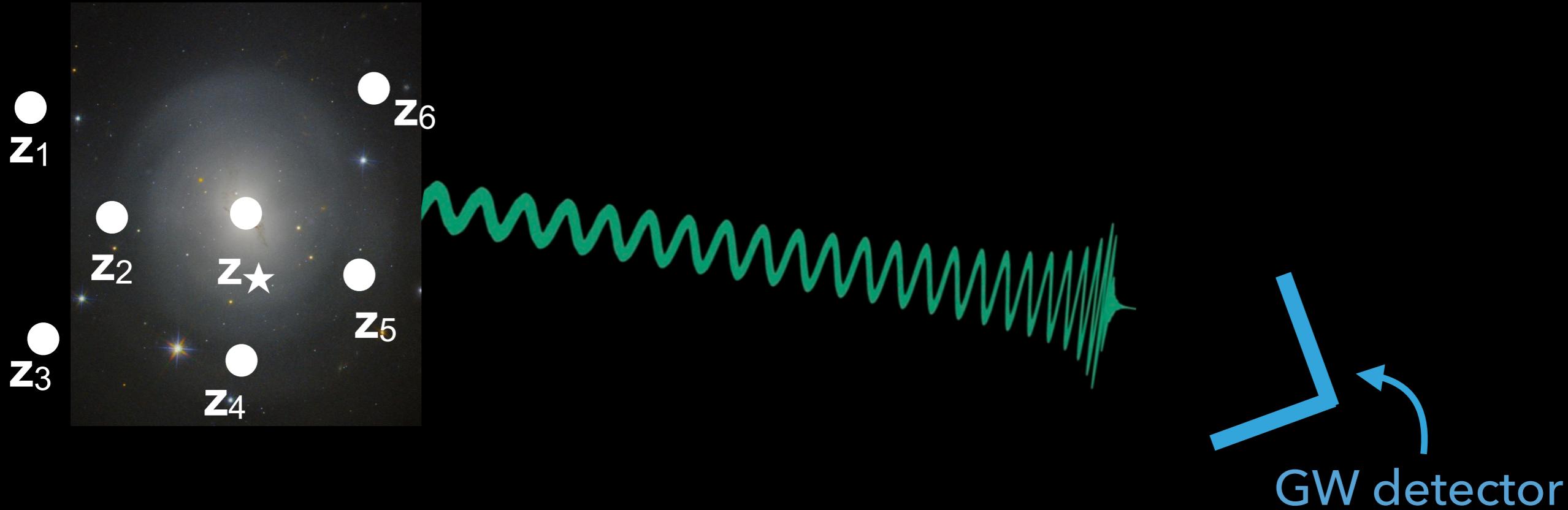
BRIGHT SIREN

Standard siren with electromagnetic counterparts—determine the redshift of gravitational-wave source with the *host galaxy*



$$H(z) = H_0 \sqrt{\Omega_M(1+z)^3 + \Omega_k(1+z)^2 + \Omega_\Lambda(1+z)^{3(1+w_0+w_a)} e^{-3w_a z/(1+z)}}$$

When there's no electromagnetic counterpart—it's difficult to identify the host galaxy



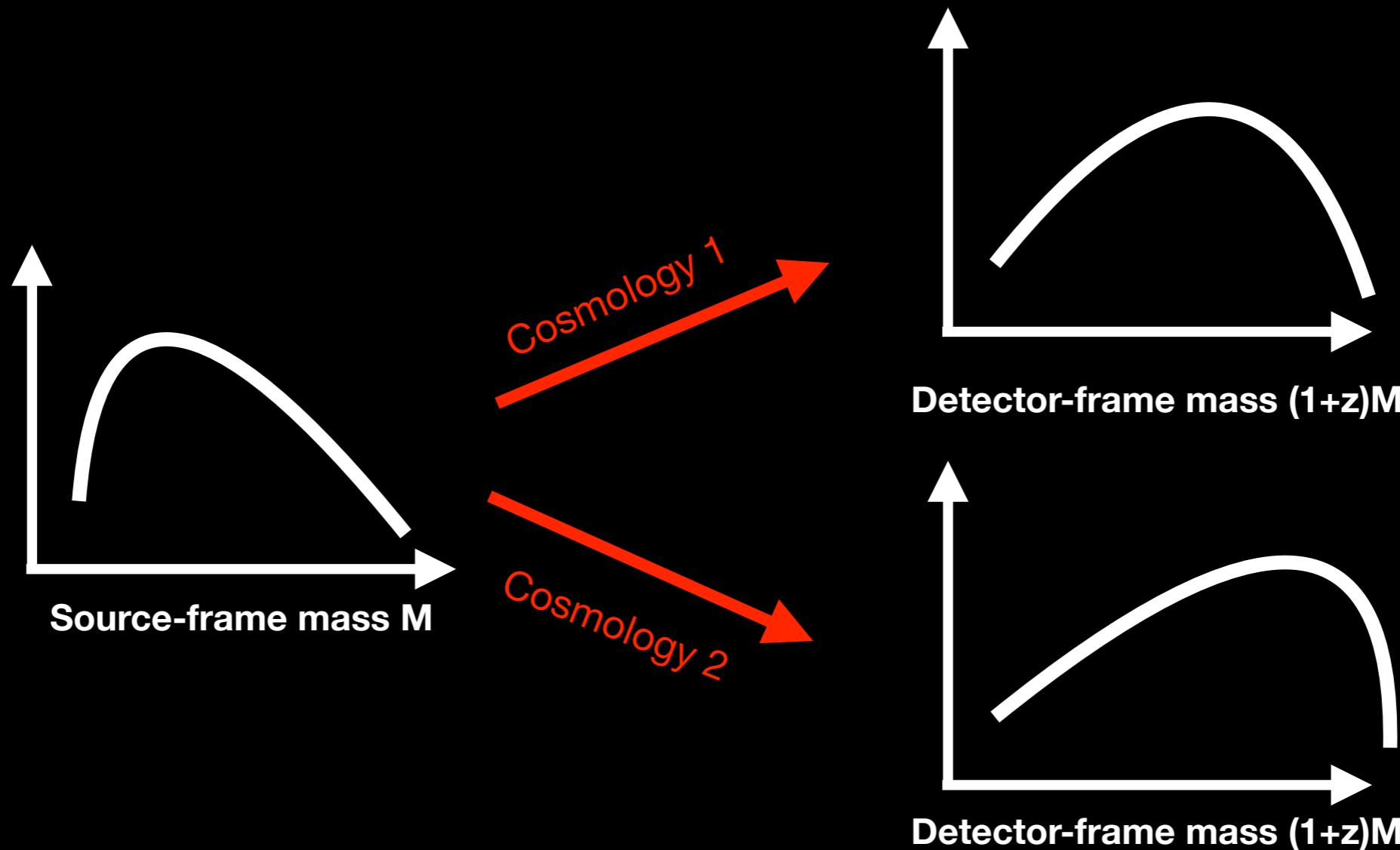
Combine the redshifts of all possible host galaxies.

Schutz, Nature, 1986/ Del Pozzo, PRD, 2011

Heavily relies on the availability/completeness of galaxy catalog.

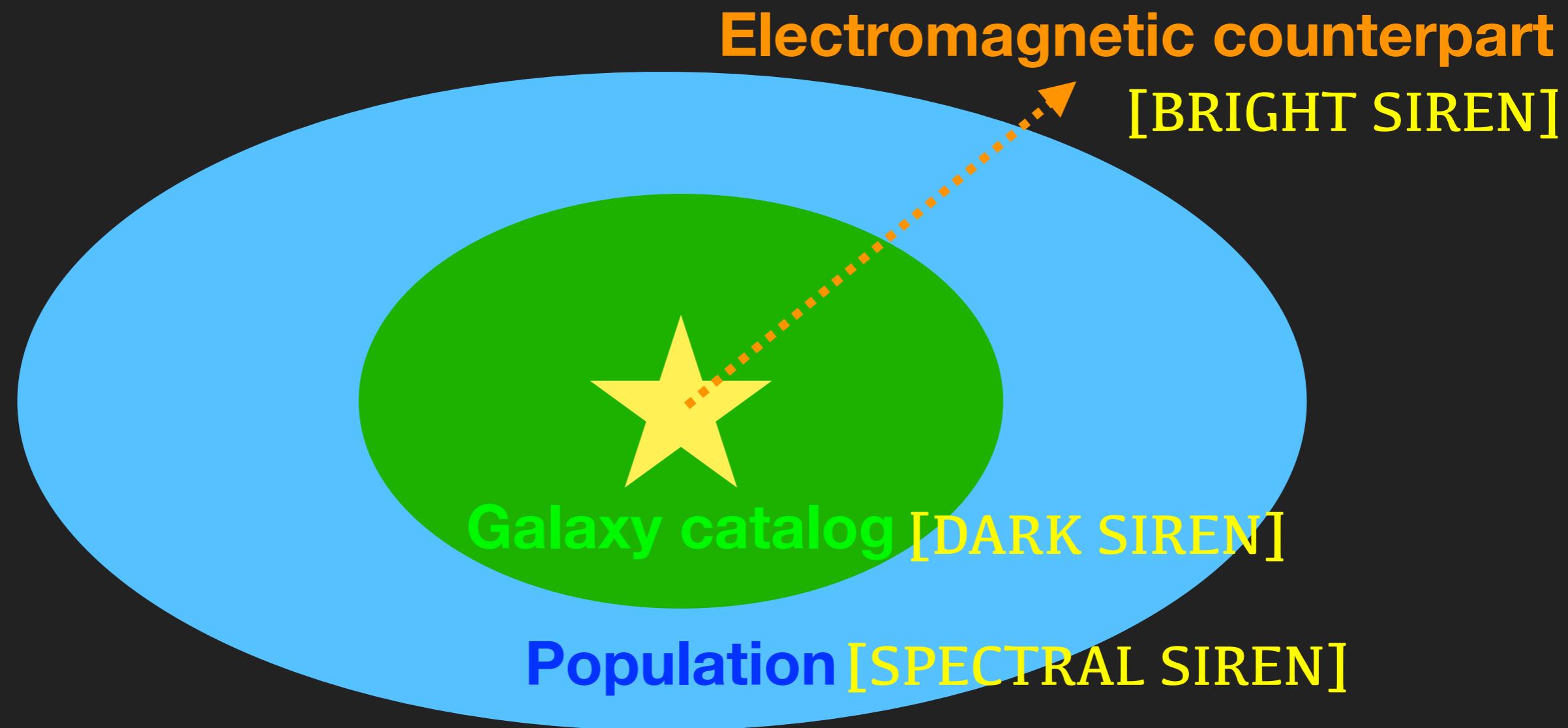
SPECTRAL SIREN

The detected mass and distance distribution of the binaries carries cosmological information too

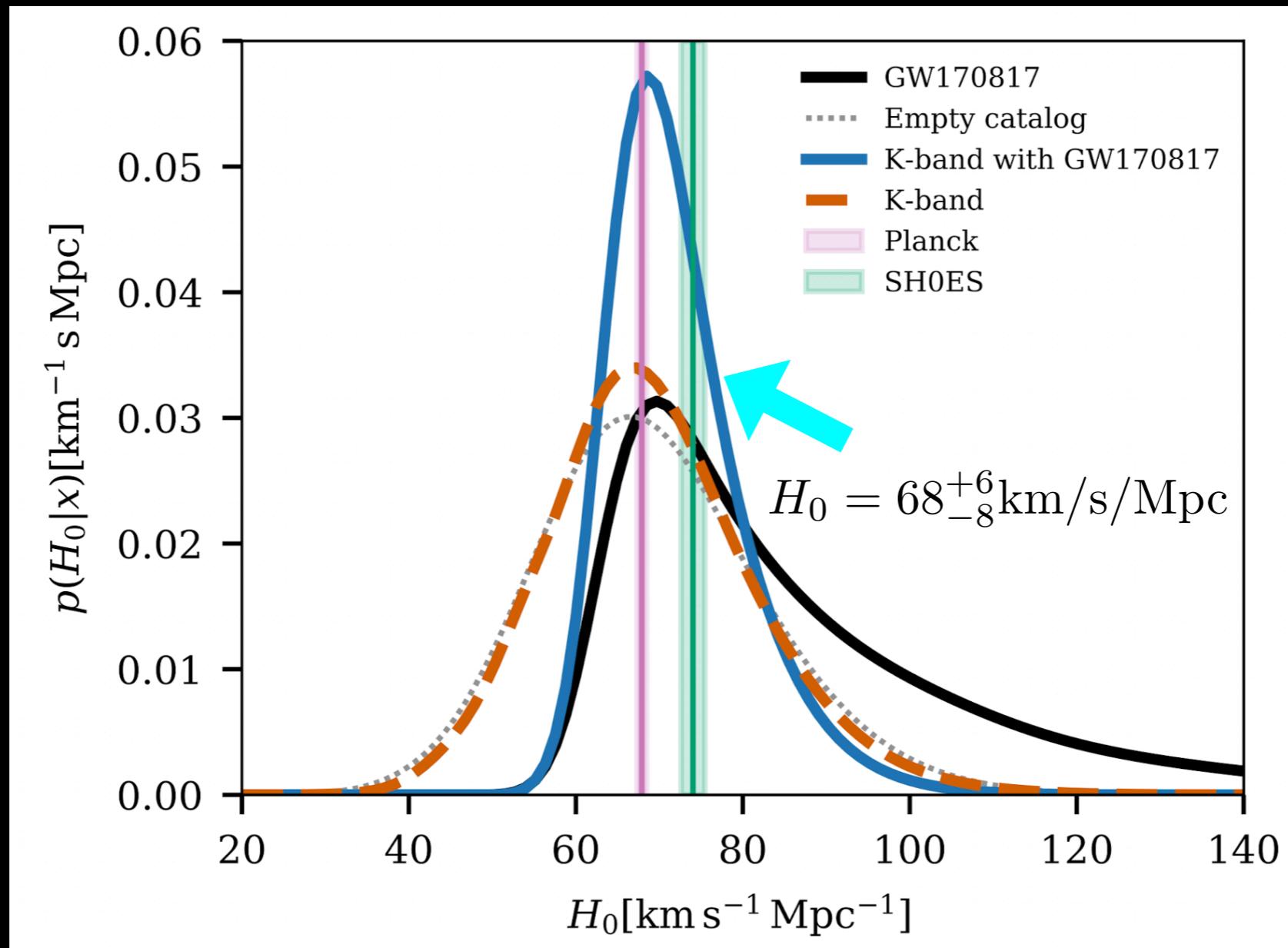


Taylor et al., PRD, 2012/Farr et al., ApJL, 2019/Mastrogiovanni, PRD, 2021/ Ezquiaga&Holz, PRL, 2022

The analysis of the data to be used to infer the cosmological and population parameters have to be consistent to be inferred jointly.



Latest LIGO-Virgo-KAGRA standard siren measurement



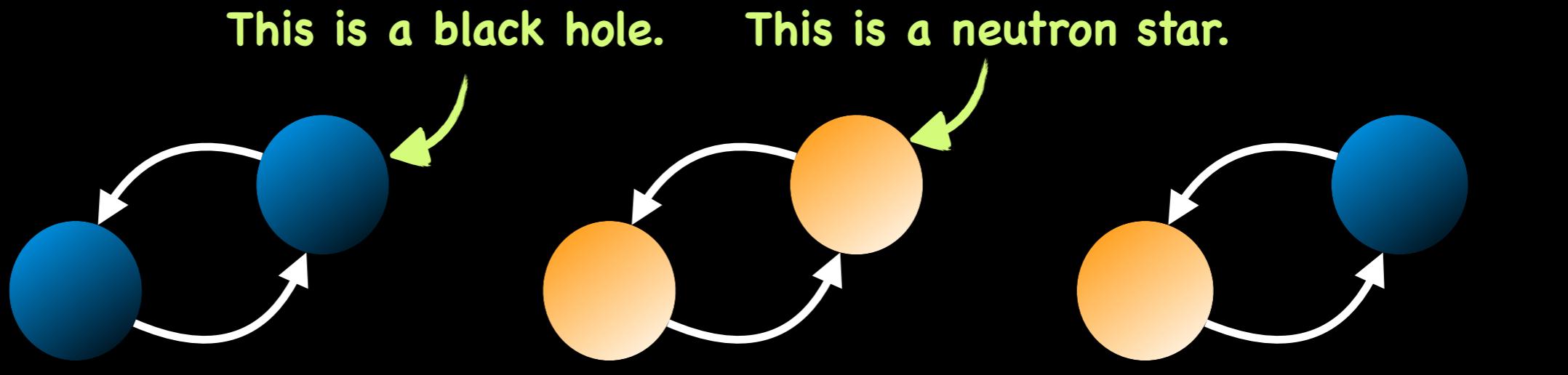
Discovery of 42 binary black hole mergers + $\int_0^z c(1+z') dz'$ LVK, 2111.03604
 $+ 2$ neutron star-black hole mergers + **GW190814**
 $H(z) = H_0 \sqrt{\Omega_M(1+z)^3 + \Omega_k(1+z)^2 + \Omega_\Lambda(1+z)^{3(1+w)}}$

What will be different in the LISA era?

Standard siren sources

Gravitational-wave sources for standard sirens

LIGO



**Extreme mass-
ratio inspiral**

LISA



**Stellar-origin
black hole binary**

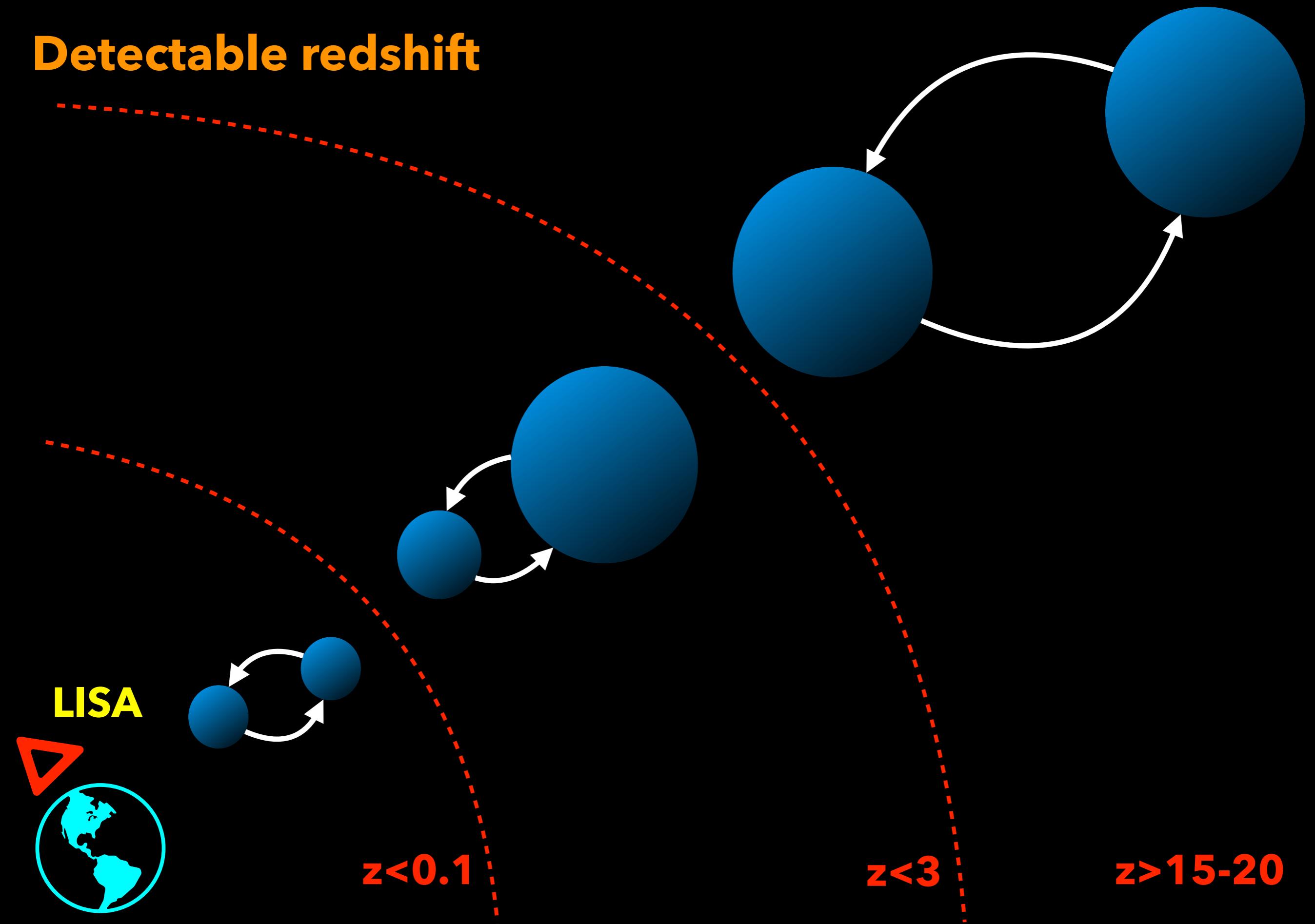
**Massive black
hole binary**

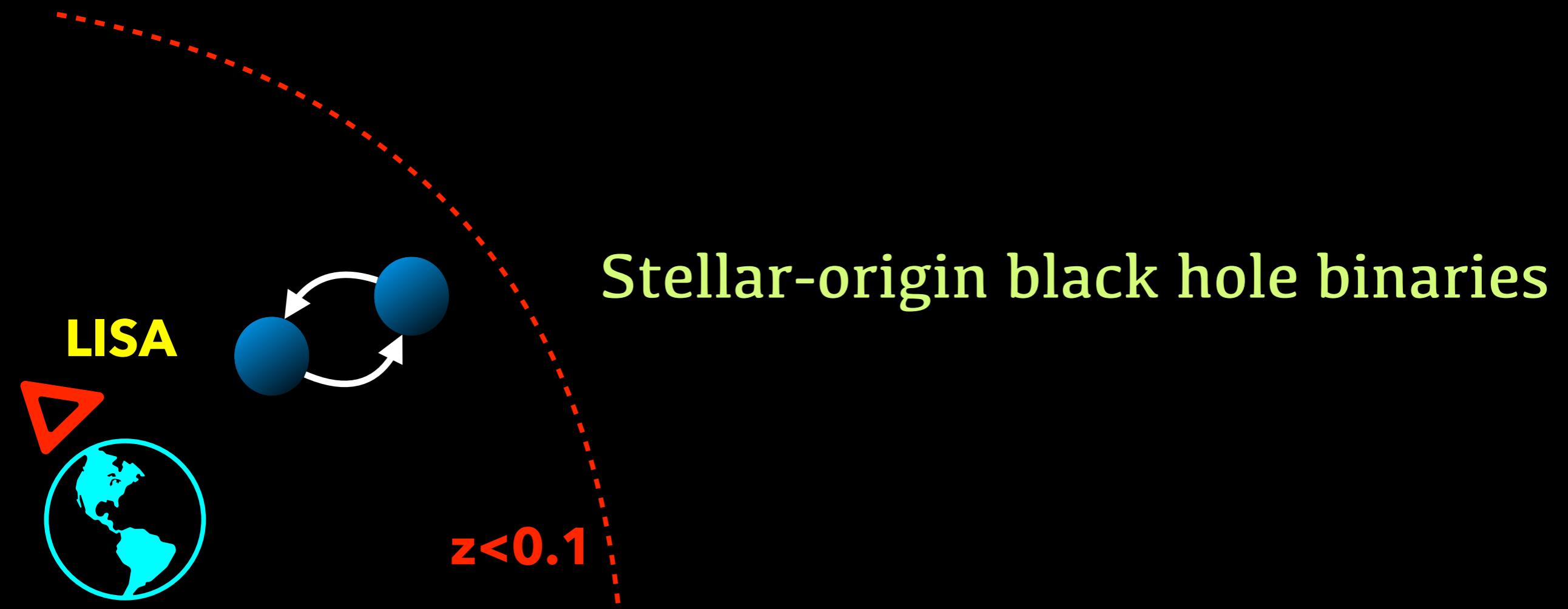
What will be different in the LISA era?

Standard siren sources

Redshift range

Detectable redshift





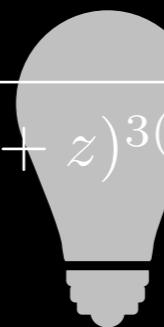
Stellar-origin binary black hole binaries

-LISA will detect them in the local Universe
 → **Best for H_0 measurement**

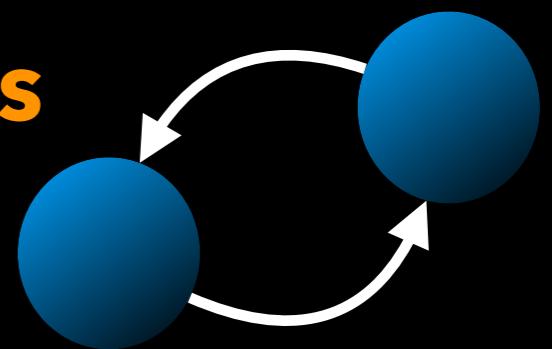
-No widely accepted electromagnetic counterpart identified so far → **Dark Siren**

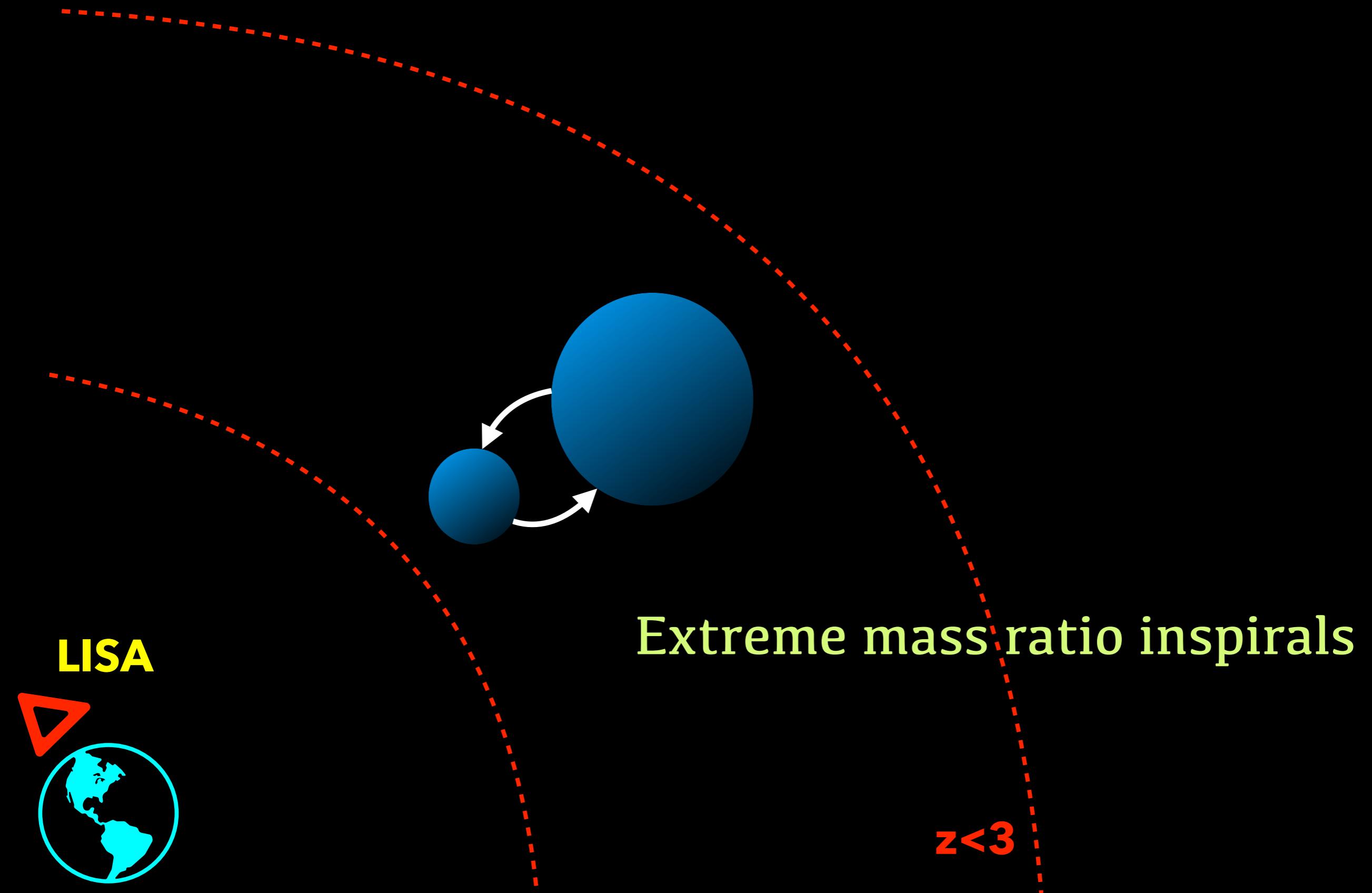
$$H(z) = H_0 \sqrt{\Omega_M(1+z)^3 + \Omega_k(1+z)^2 + \Omega_\Lambda(1+z)^{3(1+w)}}$$

[Need further verification: intermediate-mass black hole mergers may produce light.]



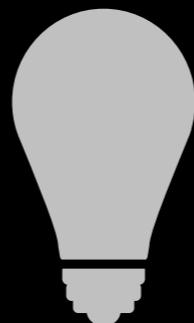
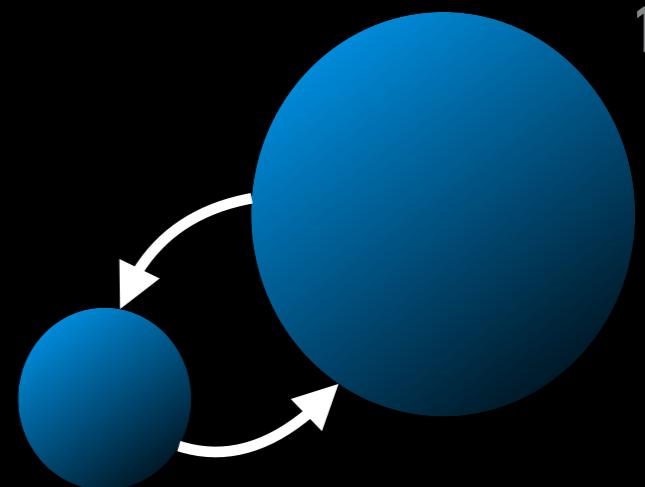
Graham et al., PRL (2020)

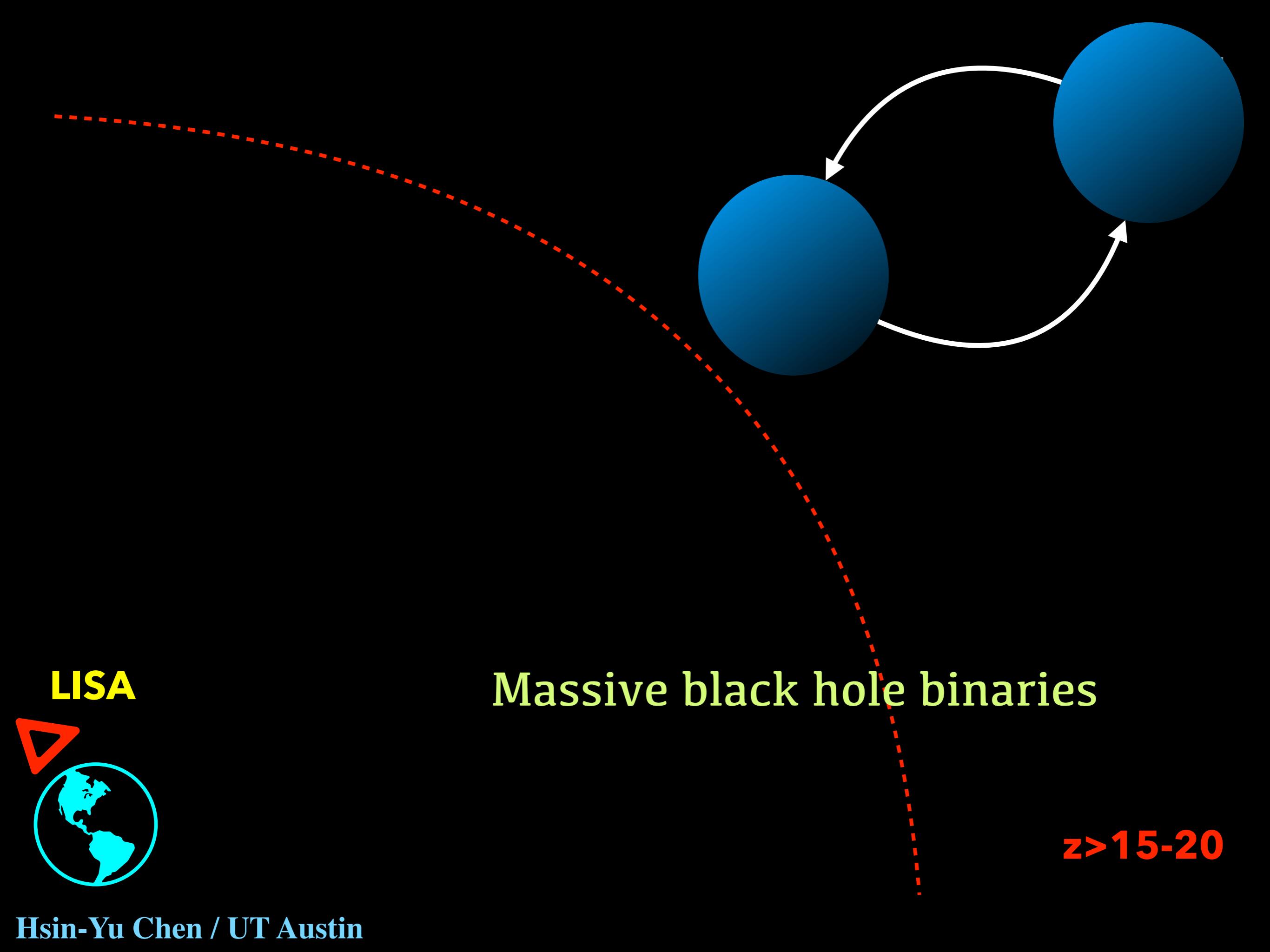




Extreme mass ratio inspirals

- LISA will detect them further away
- **Measurement of dark energy equation-of-state (w) in addition to H_0**
- No electromagnetic counterpart expected
- **Dark Siren**





LISA



Massive black hole binaries

$z > 15-20$

Massive black hole binaries

-LISA will detect them up to $z=15-20$

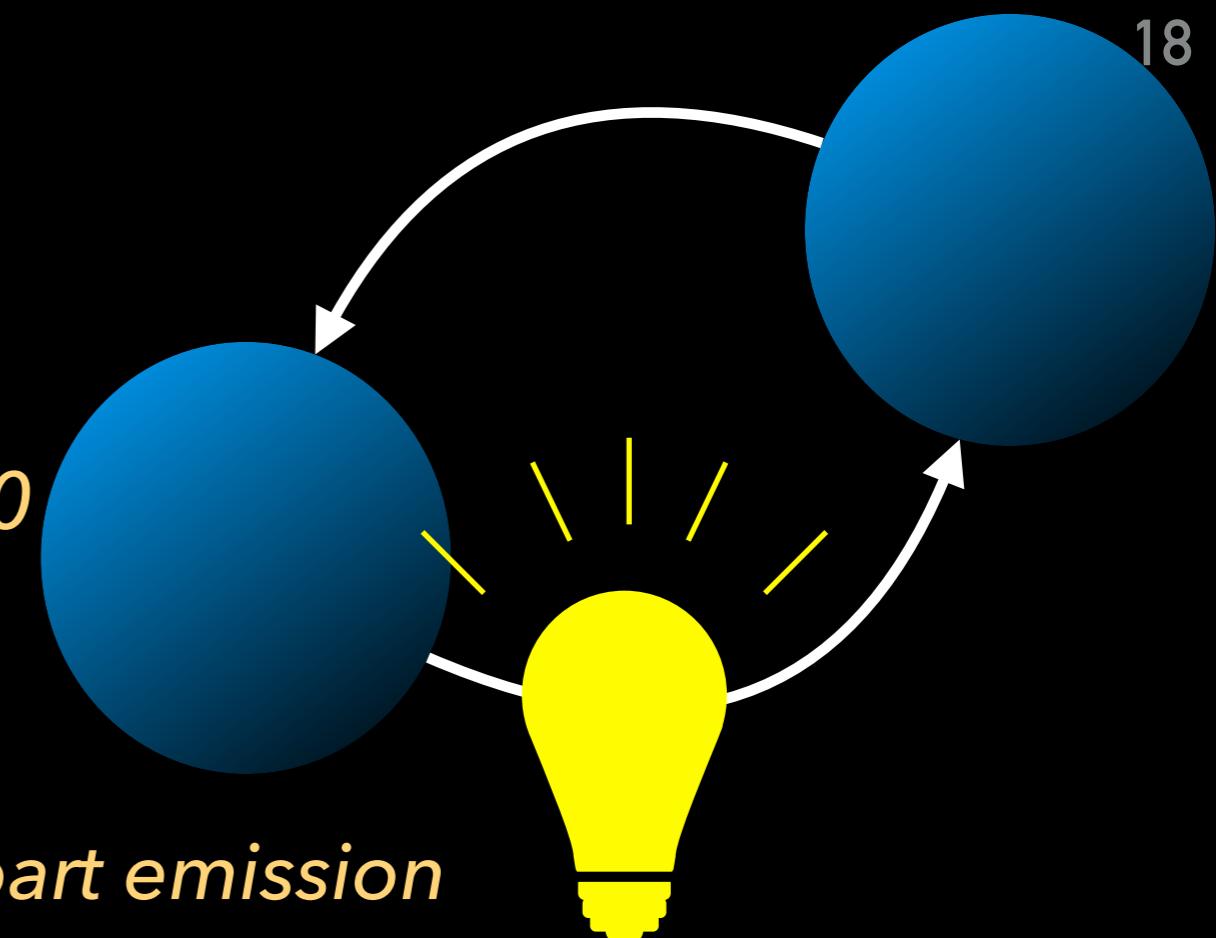
→ Constraint on $H(z)$ at high z

-Potential electromagnetic counterpart emission
in optical/x-ray/radio → **Bright Siren**

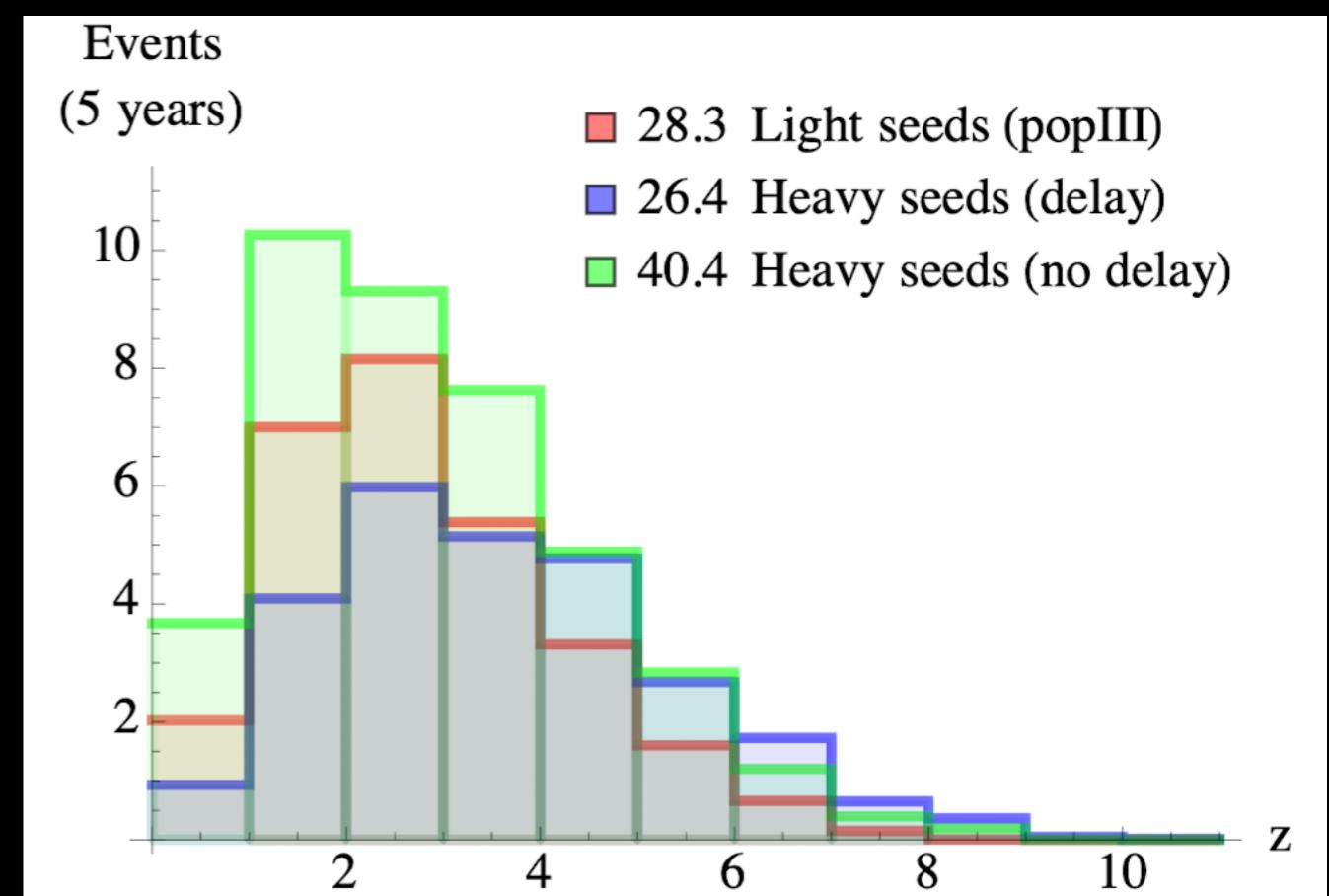
-The number of bright sirens
is highly uncertain:

-Black hole seeding models

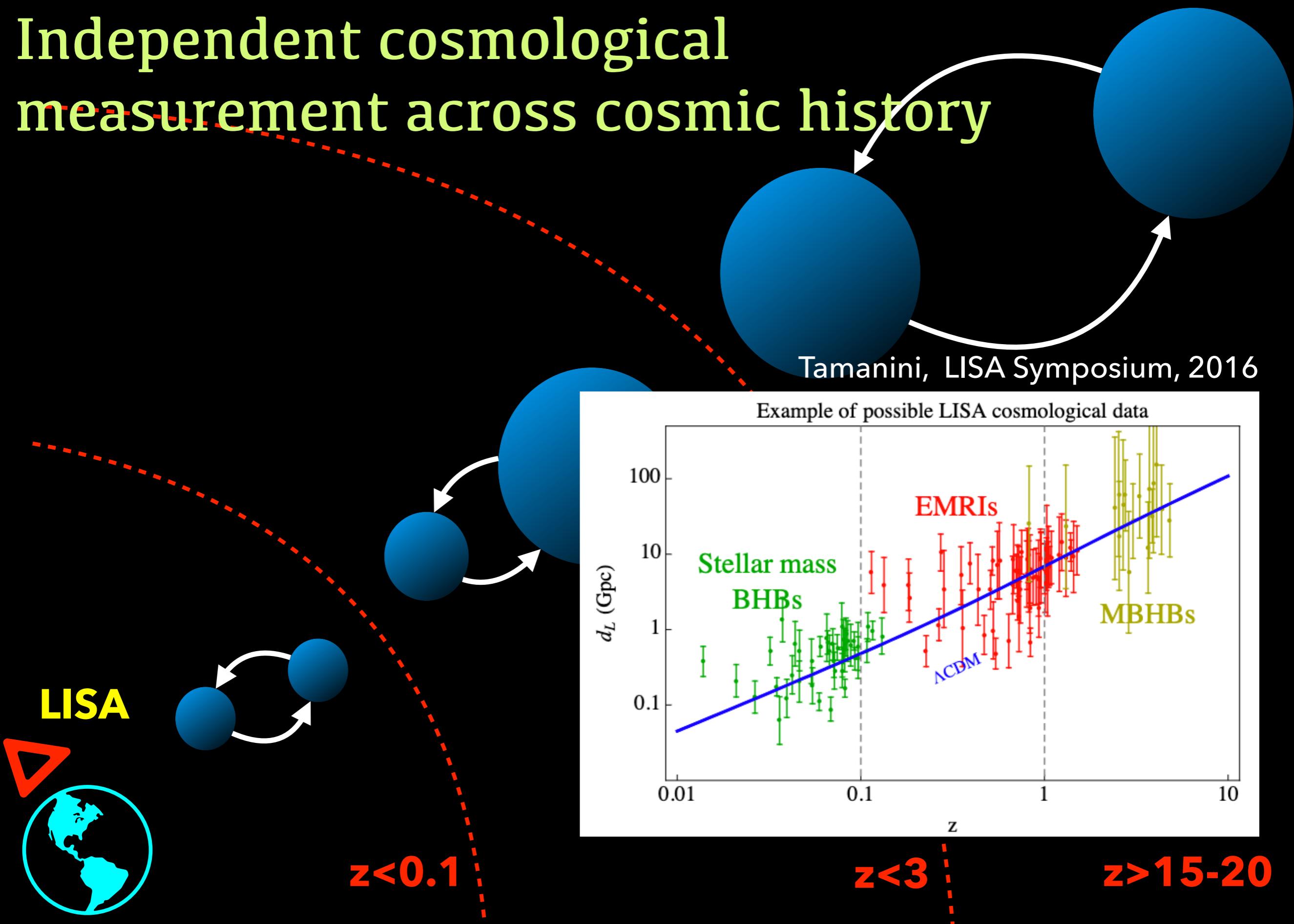
-EM emission models



Tamanini et al., JCAP, 2016



Independent cosmological measurement across cosmic history



Accuracy of the measurements

Systematic uncertainties

Potential sources of systematics

Distance

waveform

calibration

Lensing

Population

Population distribution

EM selection

Potential sources of systematics

Distance

waveform

calibration

Lensing

Population

Population distribution

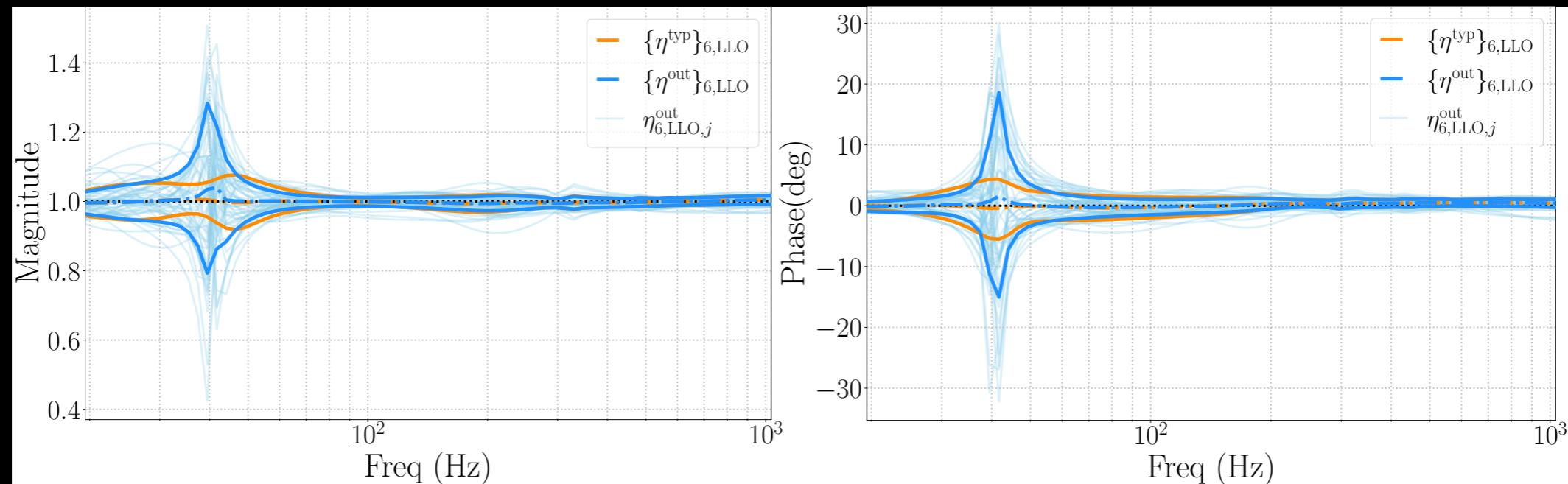
EM selection

Systematics associated with the distance measurement

Instrumental calibration uncertainty

Sun et al., CQG (2020) / Sun et al., 2107.00129

-Imperfect conversion from the voltage signals to the data stream.



Potential sources of systematics

Distance

waveform

calibration

Lensing

Population

Population distribution

EM selection

Systematics associated with the distance measurement

Weak Lensing

$$-D'_L = (1 - \kappa)D_L$$

κ is the convergence for the lensing by large scale structure

-2% for $z < 1$, 5% at $z = 2$

-Can be reduced with galaxy survey

Hilbert et al, MNRAS (2011)/ Hilbert et al, PRD (2010)

-Selection effect for high-redshift sources

Cusin and Tamanini, MNRAS (2021)

-Redshift+LISA luminosity distance measurement can be used to constrain the clustering parameters.

Cutler and Holz, PRD (2009)/Camera and Nishizawa, PRL (2013)/ Congedo and Taylor, PRD (2019)

Potential sources of systematics

Distance

waveform

calibration

Lensing

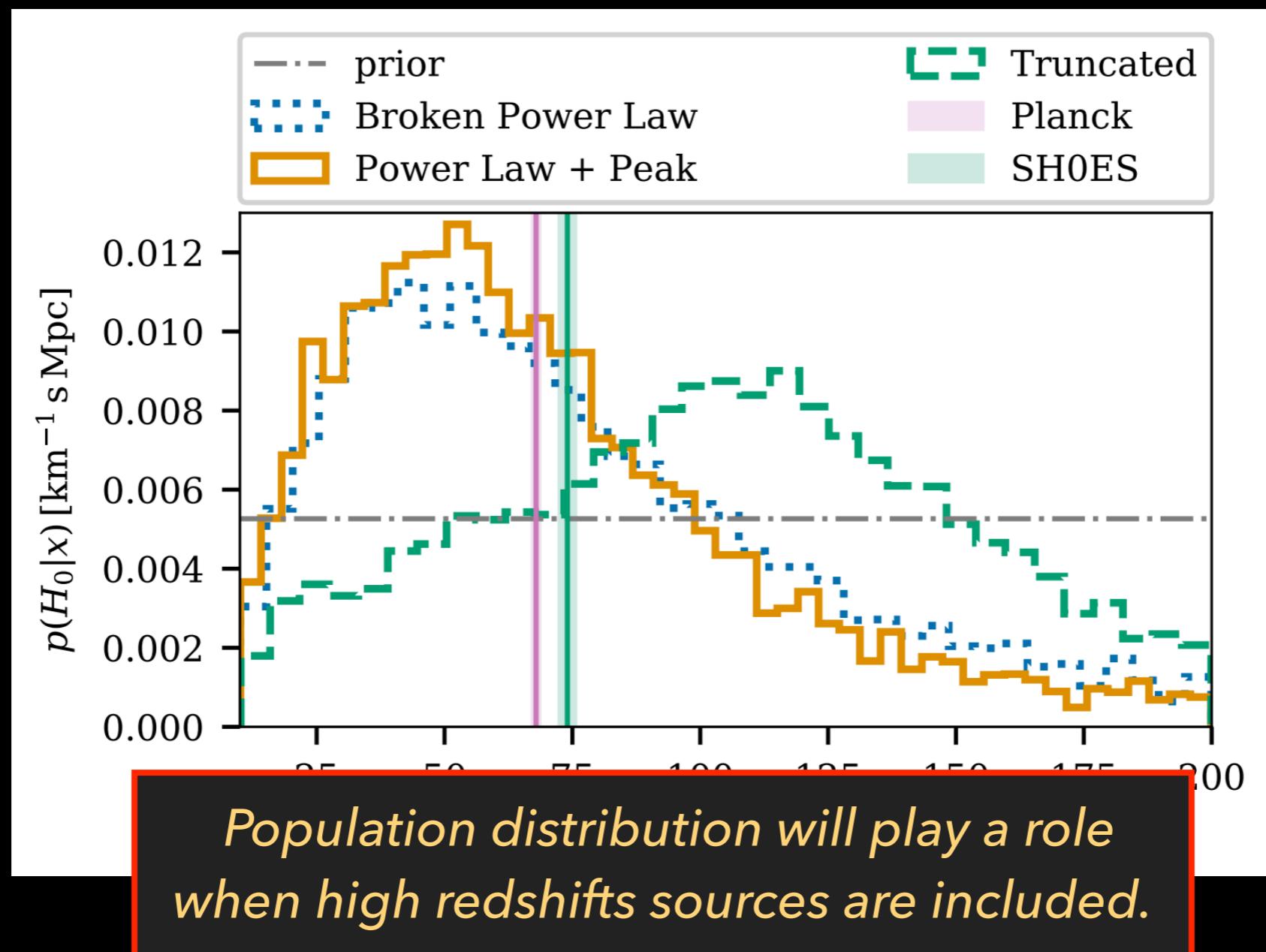
Population

Population distribution

EM selection

Systematics associated with the population

Distribution of the merger population



Potential sources of systematics

Distance

waveform

calibration

Lensing

Population

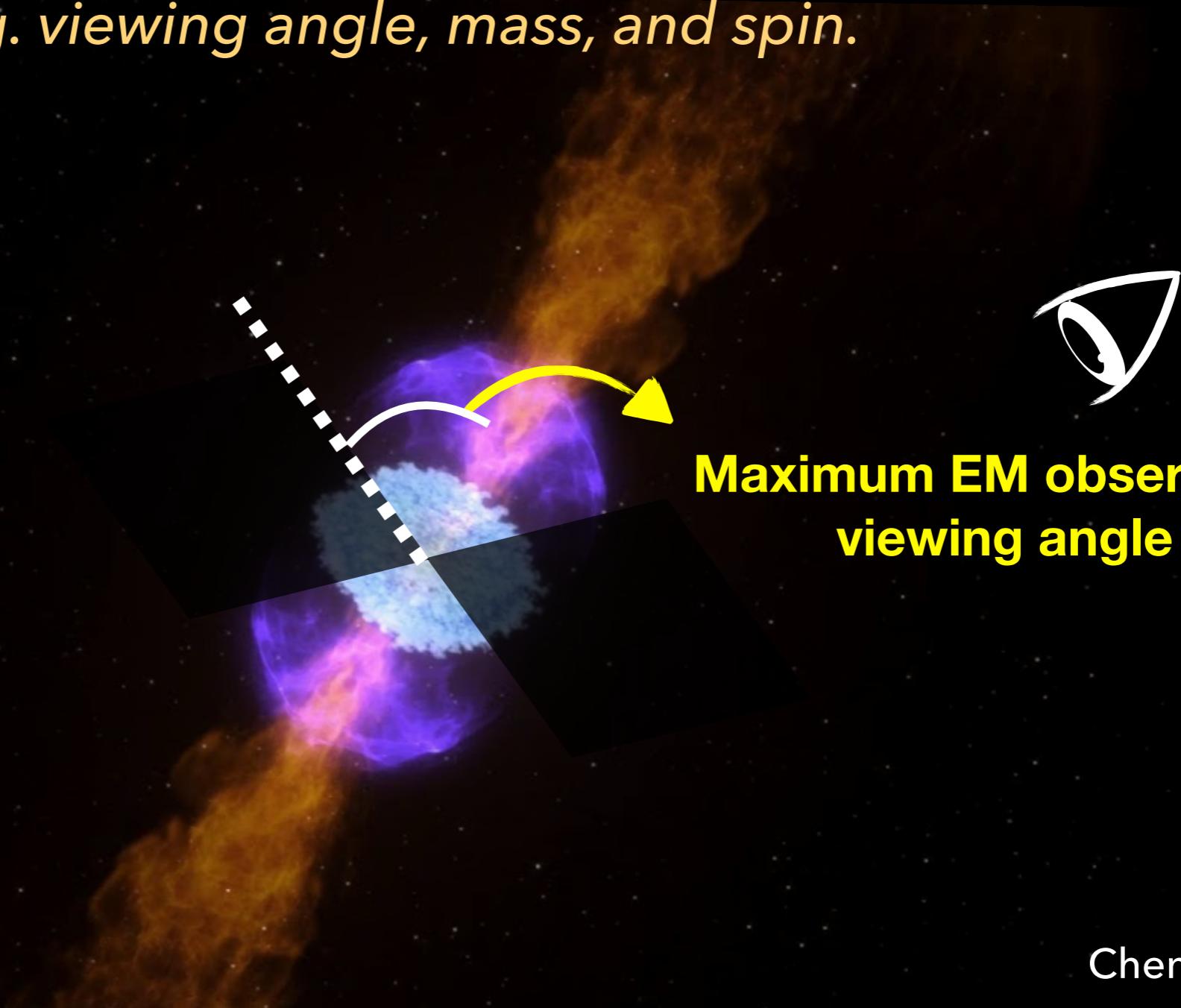
Population distribution

EM selection

Systematics associated with the population

Counterpart selection effect

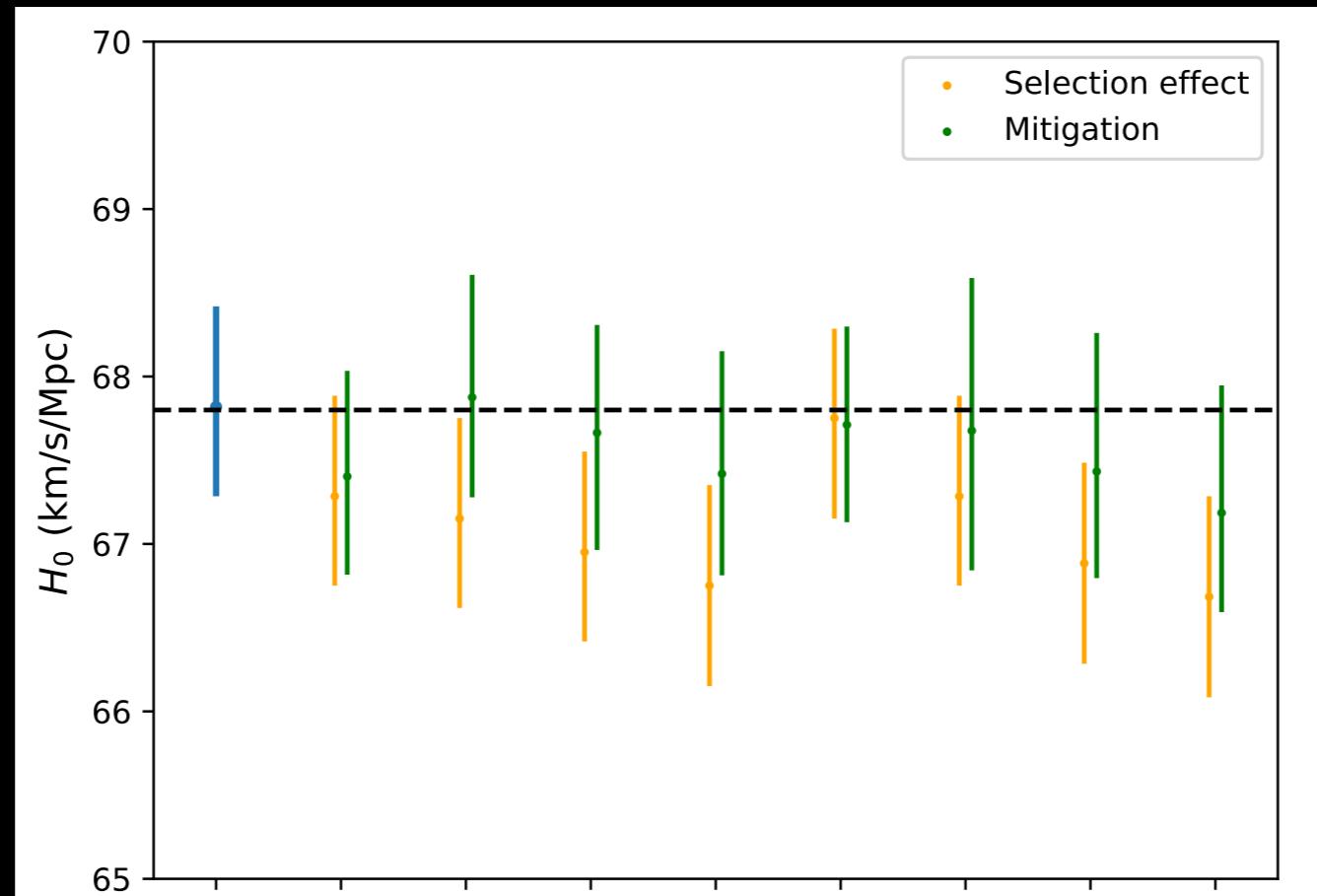
-Variation of counterpart observability as a function of the binary parameters, e.g. viewing angle, mass, and spin.



Systematics associated with the population

Counterpart selection effect

-Variation of counterpart observability as a function of the binary parameters, e.g. viewing angle, mass, and spin.



Mitigation of the effect could be easier for LISA given better parameter estimation.

Potential sources of systematics

Distance

waveform

calibration

Lensing

We currently are lack of comprehensive estimate/mitigation for many of these systematics in standard siren measurements.

Population

Population distribution

EM selection

Science Objectives of the WP

- Map the expansion rate of the Universe at all redshifts
- Test the standard cosmological model

Available Tools: for LISA

CosmoLISA

Laghi et al, MNRAS (2021)

-LISA (and 3G) bright and dark siren forecast.

-Publicly available: github.com/wdpozzo/cosmolisa

Laghi & Del Pozzo

-Proposed to be a colalborative project for LISA working group.

-Still need to implement spectral siren and several necessary technical details (e.g., selection effect, incompleteness of galaxy catalogue).

Available Tools: for LIGO/Virgo/KAGRA

-ICAROGW Mastrogiovanni et al, PRD (2023)

Dark siren + Spectral siren

-GWCOSMO Gray et al, to be on arXiv

Dark siren + Spectral siren

-DarkSirensStat Finke et al, JCAP (2021)

Dark sirens and modified GW propagation.

To be developed

-Bright+dark+spectral siren inference.

-Comprehensive estimate of the systematics.

-Mitigation of the systematics.

Thank you!

Horizon/PE uncertainty for stellar mass BBH

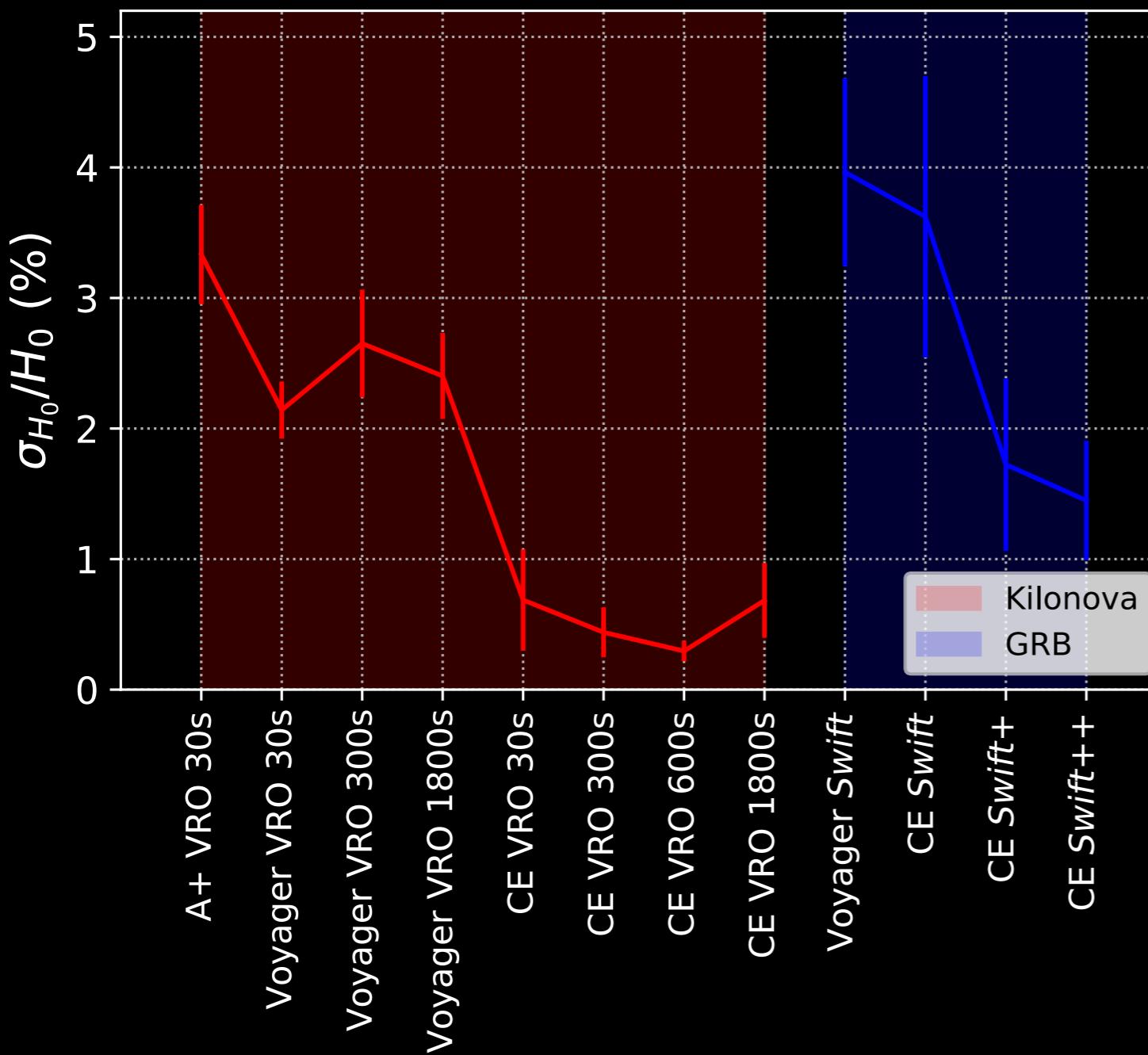
Source type	Masses [M _⊙]	red D _L [kpc]	yellow D _L [kpc]	green D _L [kpc]
BBH low	5 + 5	580	1164	2330
BBH mid	10 + 10	1849	3697	7396
GW150914	36 + 29	13031	26062	52129
GW190814	85 + 65	52875	105749	214603

Table 2: Maximum luminosity distances for $T_{\text{obs}} = 4 \text{ yr}$ (6 yr at 75% duty cycle) assuming an averaged sky location, polarization, and inclination. The green FoM is assuming the current mission design, yellow (red) is current mission design but $T_{\text{obs}} = 1 \text{ yr}$ (3 mo) to mimic sensitivity degradation

	LIGO/Virgo	ET	LISA	ET+LISA
$\Delta\Omega [\text{deg}^2]$	5.6×10^2	5.1	2.5	2.2×10^{-1}
$\Delta d_L/d_L$	3.6	3.4×10^{-1}	4.3×10^{-1}	3.9×10^{-2}
$\Delta \mathcal{M}/\mathcal{M}$	3.6×10^{-1}	3.3×10^{-3}	4.1×10^{-7}	2.0×10^{-7}
$\Delta \iota/\iota$	5.9	4.7×10^{-1}	9.3×10^{-1}	6.5×10^{-2}
$\Delta \chi_1/\chi_1$	3.9	2.8×10^{-2}	3.3×10^{-1}	8.6×10^{-4}
$\Delta \chi_2/\chi_2$	3.8	3.0×10^{-2}	4.6×10^{-1}	1.4×10^{-3}

TABLE III. Medians of the uncertainty distributions of each parameter for LIGO/Virgo, ET, LISA and the network ET+LISA, assuming 10 years LISA mission time. Here \mathcal{M} represents the *chirp mass* of the system, defined as $\mathcal{M} = (M_1 M_2)^{(3/5)} / (M_1 + M_2)^{(1/5)}$ and its uncertainty is obtained through error propagation formulas.

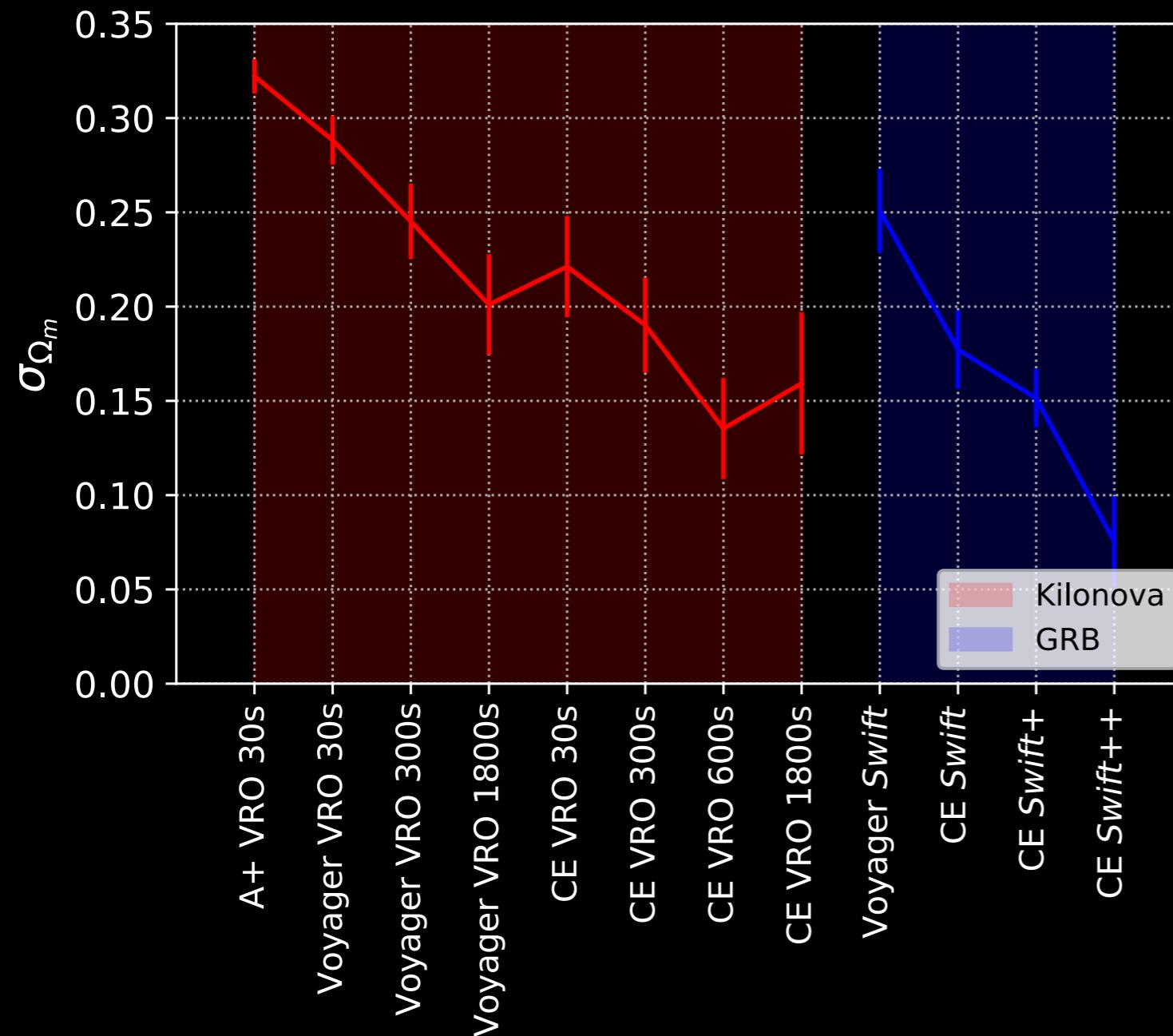
Cosmological constraints from bright sirens in 2.5-3G



-A+ and Voyager still at percent level. Sub-percent level precision is possible in CE era.

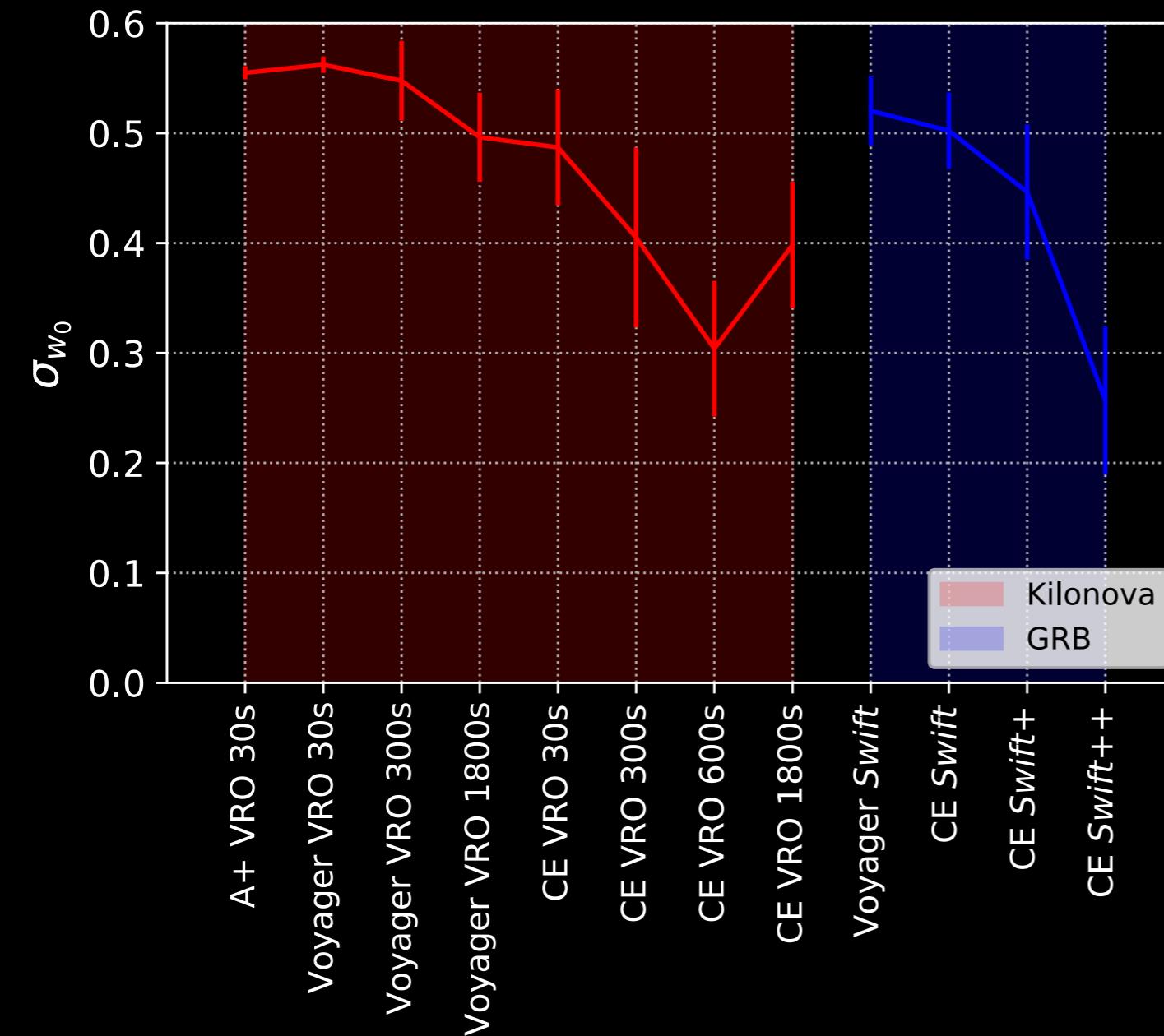
-Kilonovae are better than GRBs for H_0 constraint.

Cosmological constraints from bright sirens in 2.5-3G



- GRBs are better than kilonovae to constrain Ω_m and w .
- One order of magnitude fewer GRBs (with beaming) is needed to achieve the same precision as kilonovae.

Cosmological constraints from bright sirens in 2.5-3G



- Swift-like GRB telescope with larger field-of-view and better sensitivity is in need in the CE era.*
- Otherwise, dedicated VRO-like telescope is needed in absence of the GRB telescope described above.*

Comparison with GW/EM observations in the future

-Projection of LIGO-Virgo-KAGRA H_0 measurements

Projected Year:

